



EXPECTED ANSWERS/VALUE POINTS

SECTION - A

- | | | | |
|--------------------|-------------------|------------------|---------------------|
| 1. Terminating | 2. $x^2 - 6x + 4$ | 3. $d = 2a$ | Marks |
| | | | $1 \times 10 = 10m$ |
| 4. 1 : 9 | 5. 5cm | 6. $\frac{1}{3}$ | |
| 7. $p = 3$ | 8. (3.5) | 9. $48cm^2$ | |
| 10. $\frac{3}{26}$ | | | |

SECTION - B

11. $p(x) = x^3 - 4x^2 - 3x + 12$

$\sqrt{3}$ and $-\sqrt{3}$ are zeroes of $p(x) \Rightarrow (x^2 - 3)$ is a factor of $p(x)$ 1/2 m

$$(x^3 - 3x - 4x^2 + 12) \div (x^2 - 3) = x - 4 \quad \text{1m}$$

$\Rightarrow x = 4$ is the third zero of $p(x)$ 1/2 m

12. For a pair of linear equations to have infinitely

many solutions : $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ 1/2 m

$$\therefore \frac{\overset{(i)}{2}}{k-1} = \frac{\overset{(ii)}{3}}{k+2} = \frac{\overset{(iii)}{7}}{3k}$$

From (i) and (ii) getting $k = 7$ 1 m

$k = 7$ satisfies (ii) and (iii) and (i) and (iii) also 1/2 m

$\therefore k = 7$



13. Here $a = 2$, $l = 29$ and $s_n = 155$

$$\therefore 155 = \frac{n}{2} [2 + 29] \Rightarrow n = 10$$

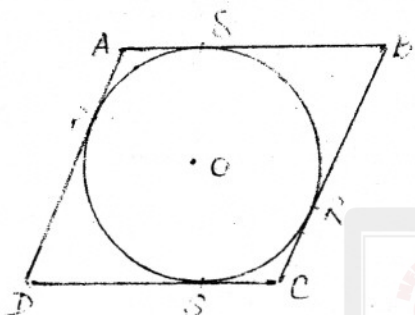
$$\text{Also, } 29 = 2 + (10 - 1)d \Rightarrow d = 3$$

\therefore Common difference = 3

1 m

1 m

14.



As parallelogram ABCD circumscribes a circle

with centre O

$$\therefore AB + CD = BC + AD$$

$$[\because AQ = AP, BQ = BR, CR = CS, PD = DS]$$

As ABCD is a parallelogram $\Rightarrow AB = DC$

and $BC = AD$

$$2AB = 2AD \text{ or } AB = AD$$

\therefore ABCD is a rhombus (As $AB = BC = CD = AD$)

$\frac{1}{2}$ m

1 m

$\frac{1}{2}$ m

15. $\sec(90^\circ - \theta) = \operatorname{cosec} \theta$, $\tan(90^\circ - \theta) = \cot \theta$, $\cos 65^\circ = \sin 25^\circ$

and $\tan 63^\circ = \cot 27^\circ$

\therefore Given expression becomes

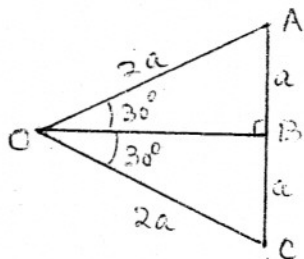
$$\frac{(\operatorname{cosec}^2 \theta - \cot^2 \theta) + (\cos^2 25^\circ + \sin^2 25^\circ)}{3 \tan 27^\circ \cot 27^\circ} = \frac{1+1}{3} = \frac{2}{3}$$

1 m

1 m

OR

correct Fig.



Draw rt. Δ OBA, in which $\angle BOA = 30^\circ$

Take $OA = 2a$. Replicate Δ OCB on

the other side of OB $\Rightarrow \angle AOC = 60^\circ$

and $OC = 2a$

$\therefore \Delta$ AOC is equilateral Δ and $AB = a$

$\frac{1}{2}$ m

$\frac{1}{2}$ m



$$\operatorname{cosec} 30^\circ = \frac{OA}{AB} = \frac{2a}{a} = 2$$

$$\therefore \operatorname{cosec} 30^\circ = 2$$

1 m

SECTION-C

16. Let $2 - 3\sqrt{5} = x$, where x is a rational number

½ m

$$\therefore 2 - x = 3\sqrt{5} \text{ or } \frac{2-x}{3} = \sqrt{5} \dots\dots\dots(i)$$

½ m

As x is a rational number, so is $\frac{2-x}{3}$

1 m

\therefore LHS of (i) is rational but RHS of (i) is irrational

\therefore Our supposition that x is rational is wrong

$\Rightarrow 2 - 3\sqrt{5}$ is irrational

1 m

17. Let the fraction be $\frac{x}{y}$, $y \neq 0$

\therefore According to the question $x + y = 2y - 3$

1 m

$$\text{or } x = y - 3 \dots\dots\dots(i)$$

$$\text{Also, } \frac{x-1}{y-1} = \frac{1}{2} \Rightarrow 2x - y = 1 \dots\dots\dots(ii)$$

1 m

From (i) and (ii), $x = 4, y = 7$

\therefore Required fraction = $\frac{4}{7}$

1 m

OR

$$\frac{4}{x} + 3y = 8 \dots\dots\dots(i), \quad \frac{6}{x} - 4y = -5 \dots\dots\dots(ii)$$

$$(i) \times 3 \Rightarrow \frac{12}{x} + 9y = 24 \text{ and } (ii) \times 2 \Rightarrow \frac{12}{x} - 8y = -10$$

1½ m

Solving to get $y = 2$ and $x = 2$

1½ m



18. $S_{10} = -150$ and $S_{20} = -(150+550) = -700$

$\therefore -150 = 5(2a + 9d)$ and $-700 = 10(2a + 19d)$

$\Rightarrow 2a + 9d = -30$ and $2a + 19d = -70$

$\Rightarrow d = -4$ and $a = 3$

\therefore A.P is $3, -1, -5, \dots$

1m

1m

½ m

19. $AB^2 = AC^2 + BC^2$ (i) and $AD^2 = AC^2 + DC^2$

$= AC^2 + \frac{BC^2}{4} \left(\because DC = \frac{1}{2} BC \right)$

1+½ m

or $4AD^2 = 4AC^2 + BC^2$ (ii)

½ m

From (i) and (ii), $AB^2 = AC^2 + 4AD^2 - 4AC^2$

or $AB^2 = 4AD^2 - 3AC^2$

1 m

20. The given expression can be written as

$$\frac{\frac{\sin A}{\cos A}}{1 - \frac{\cos A}{\sin A}} + \frac{1}{\frac{\sin A}{\cos A} \left(1 - \frac{\sin A}{\cos A} \right)}$$

1 m

$$= \frac{\sin^2 A}{\cos A (\sin A - \cos A)} + \frac{\cos^2 A}{\sin A (\cos A - \sin A)}$$

½ m

$$= \frac{\sin^3 A - \cos^3 A}{\sin A \cos A (\sin A - \cos A)} = \frac{\sin^2 A + \cos^2 A + \sin A \cos A}{\sin A \cos A}$$

1 m

$= \tan A + \cot A + 1$

½ m

OR



$$\text{LHS} = \left(\frac{1}{\sin A} - \sin A \right) \left(\frac{1}{\cos A} - \cos A \right)$$

$$= \frac{1 - \sin^2 A}{\sin A} \cdot \frac{1 - \cos^2 A}{\cos A} = \frac{\cos^2 A}{\sin A} \cdot \frac{\sin^2 A}{\cos A} = \sin A \cos A \quad 1\frac{1}{2} \text{ m}$$

$$= \frac{\sin A \cos A}{\sin^2 A + \cos^2 A} = \frac{1}{\frac{\sin^2 A}{\sin A \cos A} + \frac{\cos^2 A}{\sin A \cos A}} = \frac{1}{\tan A + \cot A} = \text{RHS} \quad 1 \text{ m}$$

21. Correct construction of triangle ΔABC 1 m

Correct construction of triangle similar to ΔABC 2m

22. $\frac{AP}{AB} = \frac{1}{3} \Rightarrow \frac{AP}{PB} = \frac{1}{2}$ 1/2 m



$$x = \frac{4+5}{3} = 3, \quad y = \frac{-8+2}{3} = -2 \Rightarrow P(3, -2) \quad 1+\frac{1}{2} = 1\frac{1}{2} \text{ m}$$

P lies on $2x - y + k = 0 \Rightarrow 6 + 2 + k = 0 \Rightarrow k = -8$ 1 m

23. $\begin{array}{c} \bullet \text{---} \bullet \text{---} \bullet \\ \text{P}(a, b) \quad \text{R}(x, y) \quad \text{Q}(b, a) \end{array}$ } 1/2 m

If P, R, Q are collinear, $\text{ar}(\Delta PRQ) = 0$

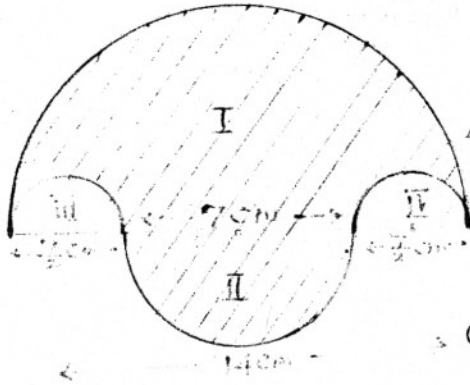
$$\therefore a(y - a) + x(a - b) + b(b - y) = 0 \quad 1 \text{ m}$$

or $ay - a^2 + ax - bx + b^2 - by = 0$

or, $(a - b)(x + y) = a^2 - b^2$ 1 m

$$\Rightarrow x + y = a + b \quad 1/2 \text{ m}$$

24.



$$\begin{aligned} \text{Area of semi-circle I} &= \frac{1}{2} \times \frac{22}{7} \times 7 \times 7 \text{ cm} \\ &= 77 \text{ cm}^2 \end{aligned}$$



$$\begin{aligned} \text{Area of semi-circle II} &= \frac{1}{2} \times \frac{22}{7} \times \frac{7}{2} \times \frac{7}{2} \text{ cm}^2 \\ &= \frac{77}{4} \text{ cm}^2 \end{aligned} \quad \frac{1}{2} \text{ m}$$

∴ Combined area of semi-circles III and IV

$$= \frac{22}{7} \times \frac{7}{4} \times \frac{7}{4} \text{ cm}^2 = \frac{77}{8} \text{ cm}^2 \quad 1 \text{ m}$$

$$\therefore \text{Area of shaded region} = 77 \left[\frac{1}{4} - \frac{1}{8} + 1 \right] \text{ cm}^2$$

$$= \frac{693}{8} \text{ cm}^2 \text{ or } 86.625 \text{ cm}^2 \quad 1 \text{ m}$$

$$AB^2 = AC^2 + BC^2 \text{ (as } \angle ACB = 90^\circ \text{)}$$

$$= 24^2 + 10^2 = 26^2 \Rightarrow AB = 26 \text{ cm} \quad \frac{1}{2} \text{ m}$$

$$\therefore \text{Area of semi-circle ACBOA} = \left(\frac{1}{2} \times 3.14 \times 13 \times 13 \right) \text{ cm}^2 \quad 1 \text{ m}$$

$$\therefore \text{Area of } \Delta ACB = \left(\frac{1}{2} \times 24 \times 10 \right) \text{ cm} = 120 \text{ cm}^2 \quad \frac{1}{2} \text{ m}$$

$$\therefore \text{Area of shaded region} = \left[\left(\frac{1}{2} \times 3.14 \times 13 \times 13 \right) - 120 \right] \text{ cm}^2$$

$$= (265.33 - 120) \text{ or } 145.33 \text{ cm}^2 \quad 1 \text{ m}$$

25. Total number of cards = 18



(i) Prime numbers less than 15 are 3, 5, 7, 11, 13 – Five in number

½ m

$$\therefore P(\text{a prime no. less than 15}) = \frac{5}{18}$$

1m

(ii) numbers divisible by 3 and 5 is only 15 (one in number)

½ m

$$\therefore P(\text{a no. divisible by 3 and 5}) = \frac{1}{18}$$

½ m

SECTION D

26. Let the three consecutive numbers be $x, x + 1, x + 2$

1 m

According to the question

$$x^2 + (x + 1)(x + 2) = 46$$

$$\text{or } 2x^2 + 3x - 44 = 0 \Rightarrow 2x^2 + 11x - 8x - 44 = 0$$

2 m

$$\Rightarrow (x - 4)(2x + 11) = 0$$

1 m

$$\text{As } x \text{ is positive } \Rightarrow x = 4 \left(x = \frac{-11}{2} \text{ rejected} \right)$$

1 m

\therefore The numbers are 4, 5, 6

1 m

OR

Let the two numbers be x, y where $x > y$

$$\therefore x^2 - y^2 = 88 \dots\dots\dots(i)$$

$$\text{Also, } x = 2y - 5 \dots\dots\dots(ii)$$

2 m

From (i) and (ii), $(2y - 5)^2 - y^2 = 88$

$$\Rightarrow 3y^2 - 20y - 63 = 0$$

1 m

$$\text{or } 3y^2 - 27y + 7y - 63 = 0 \Rightarrow (3y + 7)(y - 9) = 0$$

$$\Rightarrow y = 9, -7/3$$

1 m

$$x = 2y - 5 = 13 \text{ or } x = -\frac{29}{3}$$

1 m

∴ The numbers are 13, 9 (Rejecting $x = \frac{-29}{3}$)

and $y = -\frac{7}{3}$)



1 m

27. Correctly stated Given, To Prove, Construction and correct Figure $(\frac{1}{2} + \frac{1}{2} + \frac{1}{2} + \frac{1}{2})$

2 m

Correct Proof

2 m

Let ABC and PQR be two similar triangles

½ m

$$\frac{\text{ar} (ABC)}{\text{ar} (PQR)} = \frac{AB^2}{PQ^2} = \frac{BC^2}{QR^2} = \frac{AC^2}{PR^2} = 1 \Rightarrow AB = PQ, BC = QR, AC = PR$$

1½ m

∴ $\Delta ABC \cong \Delta PQR$ (by SSS)

½ m

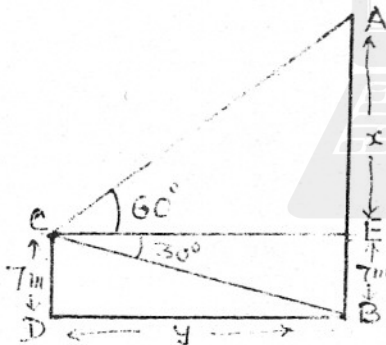
28.

Let CD be the building and AB, the tower

Correct Figure

1m

Writing trigonometric equations



$$(i) \frac{7}{y} = \tan 30^\circ = \frac{1}{\sqrt{3}} \Rightarrow y = 7\sqrt{3}$$

$$= 12.124 \text{ m} \quad 1\frac{1}{2} \text{ m}$$

$$(ii) \frac{x}{7} = \tan 60^\circ = \sqrt{3}$$

1½ m

$$\text{or } \frac{x}{7\sqrt{3}} = \sqrt{3} \Rightarrow x = 21$$

1 m

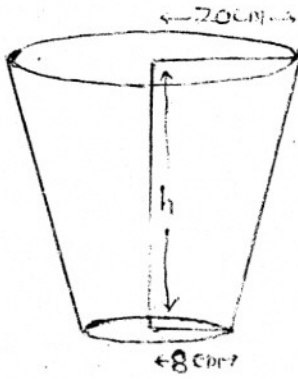
∴ Height of tower = (21 + 7) m or 28 m

1 m

29.

$$\text{Volume of bucket} = 10459 \frac{3}{7} \text{ cm}^3$$

$$= \frac{73216}{7} \text{ cm}^3$$



$$\therefore \frac{73216}{7} = \frac{1}{3} \times \frac{22}{7} \times h [20^2 + 8^2 + 20 \times 8]$$

$$\therefore h = \frac{73216}{7} \times \frac{21}{22} \times \frac{1}{624} = 16 \text{ cm} \quad 1 \text{ m}$$

$$\begin{aligned} \ell^2 &= h^2 + (r_2 - r_1)^2 = 16^2 + (20 - 8)^2 \\ &= 400 \end{aligned}$$

$$\Rightarrow \ell = 20 \text{ cm} \quad 1 \text{ m}$$

Total surface area of metal sheet used

$$\begin{aligned} &= \frac{22}{7} \times 20 \times (20 + 8) + \frac{22}{7} (8)^2 \text{ cm}^2 \\ &= \left(1760 + \frac{1408}{7} \right) \text{ cm}^2 \end{aligned} \quad \left. \vphantom{\begin{aligned} &= \frac{22}{7} \times 20 \times (20 + 8) + \frac{22}{7} (8)^2 \text{ cm}^2 \\ &= \left(1760 + \frac{1408}{7} \right) \text{ cm}^2 \right\} 2 \text{ m}$$

$$\begin{aligned} \therefore \text{Cost of metal sheet} &= \text{Rs} \left(1760 + \frac{1408}{7} \right) \frac{14}{10} \\ &= \text{Rs } 2745.60 \end{aligned} \quad 1 \text{ m}$$

OR

$$\text{Volume of hemisphere} = \frac{2}{3} \times \frac{22}{7} \times (21)^3 \text{ cm}^3 \quad 1 \text{ m}$$

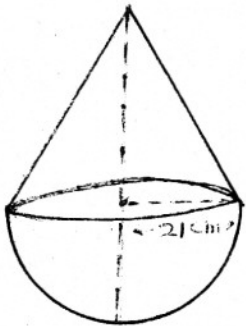
$$\therefore \text{Volume of cone} = \left(\frac{2}{3} \cdot \frac{2}{3} \cdot \frac{22}{7} \times 21 \times 21 \times 21 \right) \text{ cm}^3$$

$$= \frac{1}{3} \times \frac{22}{7} \times (21)^2 \times h \quad 1\frac{1}{2} \text{ m}$$

$$\Rightarrow h = \frac{2 \times 2 \times 22 \times 7 \times 21}{22 \times 21} = 28 \text{ cm} \quad 1 \text{ m}$$

$$\therefore \ell^2 = h^2 + r^2 = 28^2 + 21^2 = 1225 = (35)^2$$

$$\Rightarrow \ell = 35 \text{ cm} \quad 1 \text{ m}$$



$$\text{Surface area of toy} = 2\pi r^2 + \pi r l$$



$$= \left(2 \times \frac{22}{7} \times 21 \times 21 + \frac{22}{7} \times 21 \times 35 \right) \text{ cm}^2$$

1½ m

$$= 5082 \text{ cm}^2$$

30. Classes	0-10	10-20	20-30	30-40	40-50	50-60	60-70
class marks (x_i)	5	15	25	35	45	55	65
$d_i = \frac{x_i - 35}{10}$	-3	-2	-1	0	1	2	3
f_i	4	4	7	10	12	8	5
$f_i d_i$	-12	-8	-7	0	12	16	15

$$\sum f_i = 50, \quad \sum f_i d_i = 16$$

1 m

$$(i) \quad \bar{x} = 35 + \frac{16}{50} \times 10 = 38.2$$

1 m

$$(ii) \quad \text{Modal Class} = 40 - 50$$

½ m

$$\text{Mode} = 40 + \frac{12-10}{24-18} \times 10 = 43.33$$

1½ m

$$(iii) \quad \text{Median Class} = 30 - 40$$

½ m

$$\text{Median} = 30 + \frac{\frac{50}{2} - 15}{10} \times 10 = 40.00$$

1½ m

Note : If a candidate finds any two of the measures of central tendency correctly and finds the third correctly using Empirical formula, give full credit